

1. The fastest growing plant on record is a *Hesperoyucca whipplei* that grew 3.7 m in 14 days. What was its growth rate in micrometers per second?

- A) 0.26    B) 0.89    C) 1.3    D) 2.0    **E) 3.1**

$$\frac{(3.7 \text{ m})(10^6 \mu\text{m/m})}{(14 \text{ day})(86400 \text{ s/day})} = 3.1 \mu\text{m/s.}$$

2. Newton's law of universal gravitation is represented by

$$F = \frac{GMm}{r^2}$$

Here  $F$  is the magnitude of the gravitational force exerted by an object on another,  $M$  and  $m$  are the masses of the objects, and  $r$  is the distance between them. Force has the SI units  $\text{kg}\cdot\text{m}/\text{s}^2$ . What is the SI unit of the proportionality constant  $G$ ?

- A)  $\text{m}^3/\text{kg}\cdot\text{s}^2$**     B)  $\text{m}^2/\text{kg}\cdot\text{s}$     C)  $\text{m}/\text{kg}\cdot\text{s}$     D)  $\text{m}/\text{kg}\cdot\text{s}^2$     E)  $\text{m}^3/\text{kg}\cdot\text{s}$

Sorunun Gözümü,  $F = G \cdot \frac{m_1 m_2}{r^2}$   
 $\left[ \frac{\text{kg}\cdot\text{m}}{\text{s}^2} \right] = G \cdot \left[ \frac{\text{kg}^2}{\text{m}^2} \right]$   
 $G = \frac{\text{m}^3}{\text{kg}\cdot\text{s}^2}$

3. If  $\vec{a} \cdot \vec{b} = 3$  and  $|\vec{a} \times \vec{b}| = 4$ , what is the angle (in degree) between the two vectors  $\vec{a}$  and  $\vec{b}$  ?

- A) 60    **B) 53**    C) 45    D) 37    E) 30

$|\vec{a} \times \vec{b}| = ab \sin \theta = 4$   
 $\vec{a} \cdot \vec{b} = ab \cos \theta = 3$   
 $\frac{4}{3} = \frac{\sin \theta}{\cos \theta} \rightarrow \tan \theta = \frac{4}{3} \rightarrow \theta = 53^\circ$

4. When vector  $\mathbf{B}$  is added to the vector  $\mathbf{C} = 3\mathbf{i} + 4\mathbf{j}$ , the result is a vector in the positive y direction whose magnitude is equal to the magnitude of  $\mathbf{C}$ . What is the magnitude of  $\mathbf{B}$ ?

- A) 5.6    B) 1.3    **C) 3.2**    D) 4.8    E) 8.9

$\vec{R} = \vec{B} + \vec{C}$   
 $R_x \hat{i} + R_y \hat{j} = (B_x + C_x) \hat{i} + (B_y + C_y) \hat{j}$   
 $R_x = 0 \Rightarrow B_x + C_x = 0 \Rightarrow B_x = -C_x \Rightarrow \boxed{B_x = -3}$   
 $R_x^2 + R_y^2 = C_x^2 + C_y^2$   
 $R_y^2 = 9 + 16 = 25 \Rightarrow R_y = 5$   
 $R_y = B_y + C_y \Rightarrow 5 = B_y + 4 \Rightarrow \boxed{B_y = 1}$   
 $B = \sqrt{B_x^2 + B_y^2} = \sqrt{(-3)^2 + (1)^2}$   
 $\boxed{B \cong 3.2}$

5. Two vectors, of magnitudes 20 and 50, are added. Which one of the following is a possible answer for the magnitude of the resultant vector?

- A) 10 B) 20 **C) 40** D) 80 E) 100

Minimum condition:  $50-20=30$

Maximum condition:  $50+20=70$

The result of addition must be between 30 and 70

6. The vectors  $\vec{a} = 2\hat{i} - \hat{j} - \hat{k}$ ,  $\vec{b} = 2\hat{i} - \hat{j} + 3\hat{k}$  and  $\vec{c} = -2\hat{j} + \hat{k}$  are given. What is the result of the product of  $\vec{a} \cdot (\vec{b} \times \vec{c})$ ?

- A) 4 B) 8 C) 12 **D) 16** E) 20

② vektörler  
 $\vec{a} \cdot (\vec{b} \times \vec{c}) = (2\hat{i} - \hat{j} - \hat{k}) \cdot \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & -1 & 3 \\ 0 & -2 & 1 \end{vmatrix} = 16$

7. The position of a particle moving along the x-axis is given as  $x = 6t + 0.5t^3$ , where t; seconds and x; is in meters. What is the ratio of the average acceleration of this object between  $t=2$  s and  $t=4$  s to its instantaneous acceleration at  $t=2$  s?

- A) 2/3 B) 1 **C) 3/2** D) 4/3 E) 3/4

③  $x = 6t + 0,5t^3$   
 $v_x(t) = 6 + 1,5t^2$   
 $a_{x,ort} = \frac{v_{son} - v_{ilk}}{t_{son} - t_{ilk}} = \frac{\Delta v}{\Delta t}$   
 $v_x(4) = 6 + 1,5(4)^2 = 30 \text{ m/s}$   
 $v_x(2) = 6 + 1,5(2)^2 = 12 \text{ m/s}$   
 $a_{x,ort} = \frac{(30 - 12) \text{ m/s}}{(4 - 2) \text{ s}} = \boxed{9 \text{ m/s}^2}$   
 t = 2 s 'de anlık ivme  
 $a_x = \frac{dv_x}{dt} = \frac{d}{dt} (6 + 1,5t^2)$   
 $a_x = 3t$ , t = 2 s 'de  $a_x = 6 \text{ m/s}^2$   
 $\frac{a_{x,ort}}{a_x} = \frac{9}{6} = \boxed{\frac{3}{2}}$

③  $x = 6t + 0,5t^3$ , t = 2s → t = 4s  
 $v_x(t) = \frac{dx}{dt} = 6 + 1,5t^2$   
 $a_{x,avg} = \frac{v_f - v_i}{t_f - t_i} = \frac{\Delta v}{\Delta t}$   
 $v_x(4) = 6 + 1,5(4)^2 = 30 \text{ m/s}$   
 $v_x(2) = 6 + 1,5(2)^2 = 12 \text{ m/s}$   
 $a_{x,avg} = \frac{(30 - 12) \text{ m/s}}{(4 - 2) \text{ s}} = \boxed{9 \text{ m/s}^2}$   
 Instantaneous acceleration at t = 2s  
 $a_x = \frac{dv_x}{dt} = \frac{d}{dt} (6 + 1,5t^2)$   
 $a_x = 3t$ , at t = 2s ⇒  $a_x = 6 \text{ m/s}^2$   
 $\frac{a_{x,avg}}{a_x} = \frac{9}{6} = \boxed{\frac{3}{2}}$

8. A student throws a set of keys vertically upwards at his sister at a window located 4 m above. The sister held the keys after 2 s. At what initial velocity were the keys thrown? ( $g=10\text{m/s}^2$ )

- A) 2 B) 8 C) 12 D) 21 E) 40

$$x = v_0 t - \frac{1}{2} g t^2$$

$$4 = v_0 2 - \frac{1}{2} 9,82^2$$

$$v_0 = 12 \text{ m/s}$$

9. A balloon is ascending vertically with a constant speed of 8 m/s. At a height of 400 m a package is released from the balloon. What is the vertical distance (in m) between the balloon and the package after 5s? ( $g=10\text{m/s}^2$ )

- A) 20 B) 40 C) 65 D) 85 E) 125

$$y_b - y_o = v_o t = 40 \text{ m}$$

$$y_p - y_o = v_o t - \frac{1}{2} g t^2 = -85 \text{ m}$$

$$\Delta y = y_b - y_p$$

$$\Delta y = 40 - (-85) = 125 \text{ m}$$

10. A car traveling at 136 km/h slows down with an acceleration of  $5 \text{ m/s}^2$  by pressing the brake. How long does it take to reach 90 km/h (in s)?

- A) 1 B) 1.4 C) 2 D) 2.6 E) 3

$$v = v_0 - at$$

$$t = \frac{v_0 - v}{a} = \frac{(136 - 90) \left( \frac{10^3 \text{ m}}{3600 \text{ s}} \right)}{5} = 2.6 \text{ s}$$

11. A particle moving along the x axis has a position given by  $x = (24t - 2t^3) \text{ m}$ , where  $t$  is measured in s. What is the magnitude of the acceleration (in  $\text{m/s}^2$ ) of the particle at the instant when its velocity is zero?

- A) 0 B) 12 C) 24 D) 36 E) 48

Don 30

$$x = 24t - 2t^3 \Rightarrow v = \frac{dx}{dt} = 24 - 6t^2 \frac{\text{m}}{\text{s}}$$

$$v = 0 \Rightarrow 24 - 6t^2 = 0 \Rightarrow t^2 = 4 \Rightarrow t = \pm 2 \Rightarrow \boxed{t = 2 \text{ s}}$$

$$a = \left. \frac{dv}{dt} \right|_{t=2\text{s}} = -12t \Big|_{t=2\text{s}} = -24 \frac{\text{m}}{\text{s}^2} \Rightarrow \boxed{|a| = 24 \frac{\text{m}}{\text{s}^2}}$$

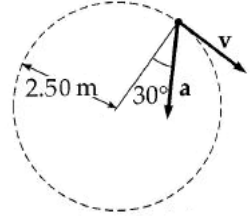
12. A basketball is thrown in such a way that its horizontal range is equal to five times its maximum height. What is the angle (in degree) of projection?. Atış açısı kaç derecedir?

- A) 25.3 B) 38.7 C) 45.0 D) 53.1 E) 77.5

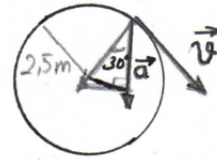
$R=5 h_{\max}$  burada R ve  $h_{\max}$  yazılıp sadeleştirme yapılırsa  $\tan\theta = 4/5$  ve  $\theta = 38.7^\circ$

13. The figure shows the net acceleration ( $a=15.0 \text{ m/s}^2$ ) and velocity of a particle moving clockwise around a 2.5 m radius circle at a given moment. Which of the following is the velocity of the particle at this instant (in m/s)?

- A) 2.35 B) 5.70 C) 6.20 D) 7.50 E) 9.15



Yandaki şekilde, belli bir anda  
2,5 m yarıçaplı daire çevresinde  
saat yönünde hareket eden bir



parçacığın net ivmesini ( $a=15 \text{ m/s}^2$ )  
ve hızını göstermektedir.  $v$  hızının büyüklüğünü bulunuz.

GÖZÜM  $a_r = a \cdot \cos 30^\circ \cong 12,99 \cong 13 \text{ m/s}^2$

$$a_r = \frac{v^2}{r} \Rightarrow v^2 = a_r \cdot r = (13 \text{ m/s}^2)(2,5 \text{ m})$$

$$v^2 = (13 \text{ m/s}^2)(2,5 \text{ m})$$

$$v = \sqrt{32,5} = 5,70 \text{ m/s.}$$

Doğru şık: B

14. Passengers on a carnival ride move at constant speed in a horizontal circle of radius 5 m, making a complete circle in 4 s. What is their acceleration in  $\text{m/s}^2$ ?

- A) 2 B) 4 C) 8 D) 12 E) 16

$$R = 5 \text{ m} \quad T = 4 \text{ s}$$

$$2\pi R = vT$$

$$v = \frac{2\pi R}{T} = \frac{2 \times 3,14 \times 5}{4}$$

$$\rightarrow v = 7,9 \text{ m/s}$$

$$a_r = \frac{v^2}{R}$$

$$a_r = \frac{(7,9)^2}{5}$$

$$a_r = 12 \text{ m/s}^2$$



15. A stone from a 45m high bridge over a river falls from rest on a small boat moving at a constant speed on the river. Since the boat is 9 m away from the meeting point when the stone starts to fall, what should the speed of the boat (m/s)? ( $g=10\text{m/s}^2$ )  
 A) 2 **B) 3** C) 6 D) 8 E) 10

Kayık için

$$x = vt$$

$$t = \frac{x}{v}$$

taş için

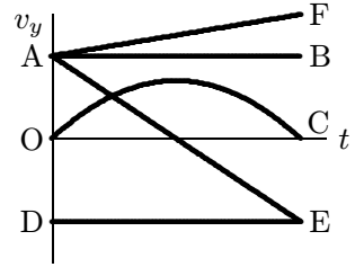
$$y = \frac{1}{2}gt^2$$

$$t = \sqrt{\frac{1}{2}g \frac{x^2}{y}}$$

$$t = \sqrt{\frac{1}{2} \cdot 9,8 \frac{9^2}{45}}$$

$$t = 2,97s$$

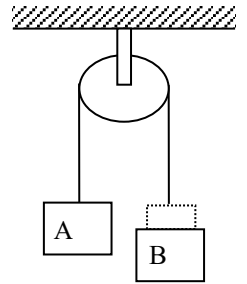
16. Which of the curves on the graph below best represents the vertical component  $v_y$  of the velocity versus the time  $t$  for a projectile fired at an angle of  $45^\circ$  above the horizontal?



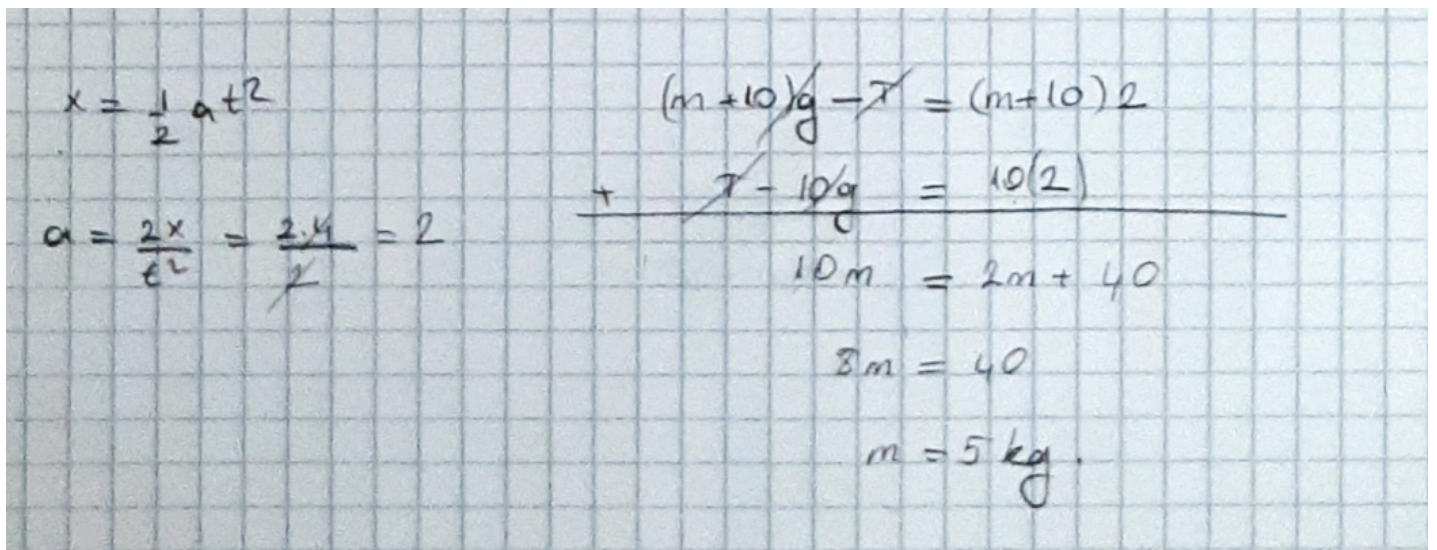
A) OC B) DE C) AB **D) AE** E) AF

**Cevap D**

17. Two objects either of which weights 10 N are connected by a rope of negligible mass. Find the weight to be added to one of the objects in order to reach 4 m in 2 s. Neglect the mass and friction of the pulley? ( $g=10\text{m/s}^2$ )



A) 1  
 B) 2  
 C) 3  
 D) 4  
**E) 5**



18. A 1.5 kg model helicopter has a velocity of  $5\mathbf{j}$  m/s at  $t=0$ . It is accelerated at a constant rate for two seconds (2.0 s) after which it has a velocity of  $(6\mathbf{i}+12\mathbf{j})$  m/s. What is the magnitude of the resultant force (in N) acting on the helicopter during this time interval?

- A) 4,8   **B) 6,9**   C) 8,2   D) 10,1   E) 12,6

We can easily set up a coordinate system in which the  $x$ -axis ( $\hat{\mathbf{i}}$  direction) is horizontal, and the  $y$ -axis ( $\hat{\mathbf{j}}$  direction) is vertical. We know that  $\Delta t = 2.00\text{ s}$  and  $\Delta v = (6.00\hat{\mathbf{i}} + 12.00\hat{\mathbf{j}} \text{ m/s}) - (5.00\hat{\mathbf{j}} \text{ m/s})$ . From this, we can calculate the acceleration by the definition; we can then apply Newton's second law.

**Solution**

We have

$$a = \frac{\Delta v}{\Delta t} = \frac{(6.00\hat{\mathbf{i}} + 12.00\hat{\mathbf{j}} \text{ m/s}) - (5.00\hat{\mathbf{j}} \text{ m/s})}{2.00 \text{ s}} = 3.00\hat{\mathbf{i}} + 3.50\hat{\mathbf{j}} \text{ m/s}^2$$

$$\sum \vec{F} = m\vec{a} = (1.50 \text{ kg})(3.00\hat{\mathbf{i}} + 3.50\hat{\mathbf{j}} \text{ m/s}^2) = 4.50\hat{\mathbf{i}} + 5.25\hat{\mathbf{j}} \text{ N}.$$

The magnitude of the force is now easily found:

$$F = \sqrt{(4.50 \text{ N})^2 + (5.25 \text{ N})^2} = 6.91 \text{ N}.$$

19.

Which of the following statements is/are correct?

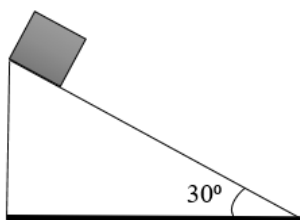
- I. The force of gravity acting on an object is called the mass of the object.
- II. Consider a body acted on by no net force. If it is at rest, it will remain at rest. If it is moving, it will continue to move with constant velocity.
- III. The coefficient of friction is a dimensionless number.

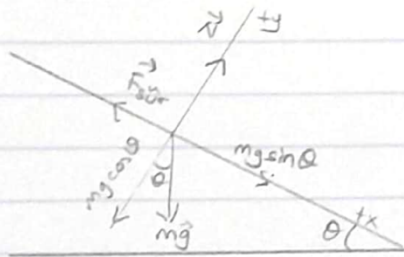
- A) I, II and III  
 B) I and II  
**C) II and III**  
 D) I and III  
 E) Yalnız III

Because it is the definition of weight, the I is wrong, the others are correct.

20. The 25 kg object in the figure slides down a rough surface at a constant speed on a slope of  $30^\circ$ . What is the value of the coefficient of kinetic friction between the object and the surface?

- A) 0,2  
**B) 0,6**  
 C) 0,9  
 D) 1,7  
 E) 2,5





$$\theta = 30^\circ$$

$$\mu_k = ?$$

$$\sum F_y = N - mg \cos \theta = m a_y = 0$$

$$\sum F_x = mg \sin \theta - F_{\text{friction}} = m a_x = 0$$

$$F_{\text{friction}} = N / \mu_k$$

$$N = mg \cos \theta$$

$$mg \sin \theta - mg \cos \theta \mu_k = 0$$

$$\mu_k = \frac{mg \sin \theta}{mg \cos \theta} = \frac{\sin \theta}{\cos \theta} = \tan \theta$$

$$\theta = 30^\circ \Rightarrow \mu_k = \tan 30^\circ$$

$$\mu_k = 0,58$$

$$\mu_k \approx 0,6$$